

Practical Round-Optimal Blind Signatures in the Standard Model from Weaker Assumptions

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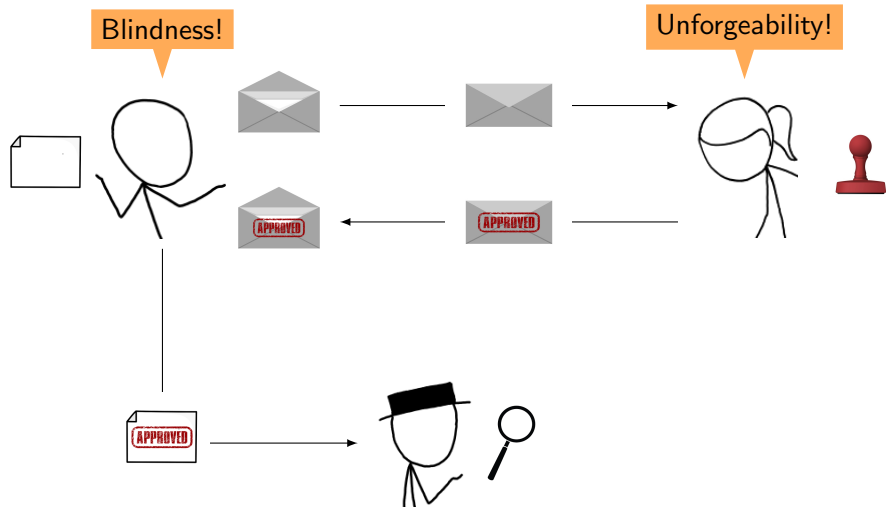
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Blind Signatures



Overview

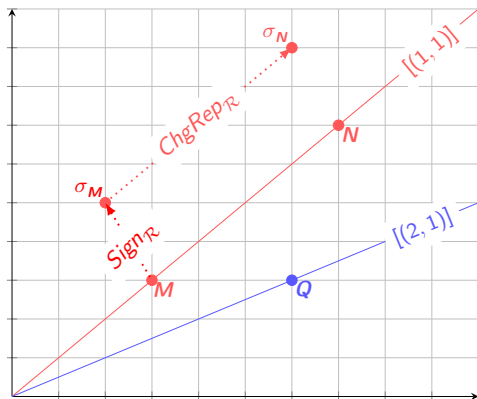
- ▶ Desiderata:
 1. Round-optimality (hence efficiency and composability)
 2. No heuristic assumptions
 3. No set-up assumptions
- ▶ Hard to construct: [FS10]
- ▶ Possibility: [GG14,GRS+11]
- ▶ First practical scheme: [FHS15]
 - ▶ SPS-EQ + commitments
 - ▶ ~~CDH~~, EUF-CMA \implies Unforgeability
 - ▶ ~~Interactive~~ variant of DDH \implies Blindness
- ▶ *Our contribution*: weaker assumptions!

Preliminaries

- ▶ Asymmetric pairing $e : \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}_T$
 - ▶ **Bilinearity:** $e(aP, b\hat{P}) = e(P, \hat{P})^{ab}$
 - ▶ **Non-degeneracy:** $e(P, \hat{P}) \neq 1_{\mathbb{G}_T}$
 - ▶ **Efficiency:** $e(\cdot, \cdot)$ efficiently computable

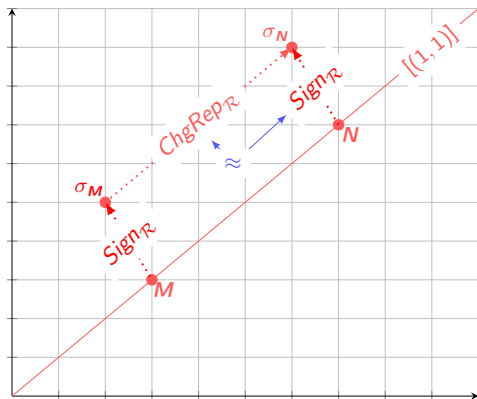
- ▶ Structure-Preserving Signatures [AFG+10]
 - ▶ Signing vector of group elements
 - ▶ Signatures and PKs consist *only* of group elements
 - ▶ Verification via
 1. pairing-product equations
 2. group membership tests

SPS on Equivalence Classes



- ▶ Equivalence relation $\sim_{\mathcal{R}}$ on \mathbb{G}^l : $\mathbf{M} \sim_{\mathcal{R}} \mathbf{N} \Leftrightarrow \exists \mu \in \mathbb{Z}_p^* : \mathbf{N} = \mu \cdot \mathbf{M}$
- ▶ SPS-EQ := SPS + “change representative” functionality

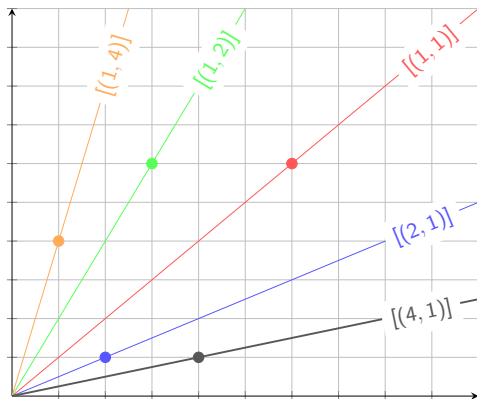
SPS-EQ: Security



- ▶ Class-hiding: $ChgRep_{\mathcal{R}}(\mathbf{M}, \sigma, \mu, \text{pk}) \approx Sign_{\mathcal{R}}(\mu\mathbf{M}, \text{sk})$
 - ▶ Malicious keys: $ChgRep_{\mathcal{R}}(\mathbf{M}, \sigma, \mu, \text{pk})$ uniform in space of signatures on $\mu\mathbf{M}$

Unforgeability: EUF-CMA w.r.t $\approx_{\mathcal{R}}$

SPS-EQ: Security



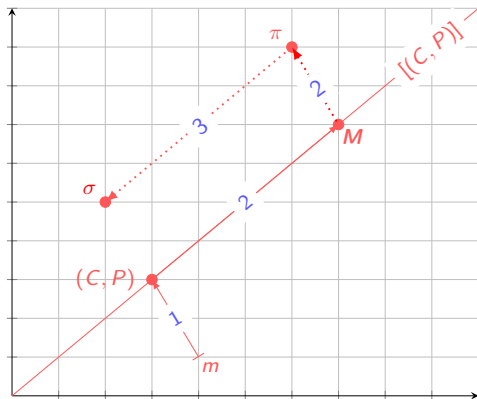
- ▶ Class-hiding: $ChgRep_{\mathcal{R}}(\mathbf{M}, \sigma, \mu, \text{pk}) \approx \text{Sign}_{\mathcal{R}}(\mu\mathbf{M}, \text{sk})$
 - ▶ Malicious keys: $ChgRep_{\mathcal{R}}(\mathbf{M}, \sigma, \mu, \text{pk})$ uniform in space of signatures on $\mu\mathbf{M}$
- ▶ Unforgeability: EUF-CMA w.r.t $\sim_{\mathcal{R}}$

Blind Signatures from SPS-EQ

FHS Blind Signature

► Bob:

1. Commits to m using Pedersen commitment $C = mP + rQ$
2. Obtains signature π from Alice on random $\mathbf{M} \sim [(C, P)]_{\mathcal{R}}$
3. Derives σ on (C, P) using $\text{ChgRep}_{\mathcal{R}}$
4. Outputs $\tau = (\sigma, \text{opening of } C)$ to Charlie



$$\text{pk} = (\text{pk}_{\mathcal{R}}, (Q, \hat{Q}) = q \cdot (P, \hat{P}))$$

Pedersen Commitment

$$m \in \mathbb{Z}_p^*$$

$$r, s \in \mathbb{Z}_p^*$$



$$M = s \cdot (mP + rQ, P)$$



$$\text{sk} = (\text{sk}_{\mathcal{R}}, q)$$

$$\pi \leftarrow \text{Sign}_{\mathcal{R}}(M, \text{sk})$$

$$\sigma \leftarrow \text{ChgRep}_{\mathcal{R}}(M, \pi, 1/s, \text{pk}_{\mathcal{R}})$$

$$\tau \leftarrow (\sigma, R = rP, T = rQ)$$

Opening

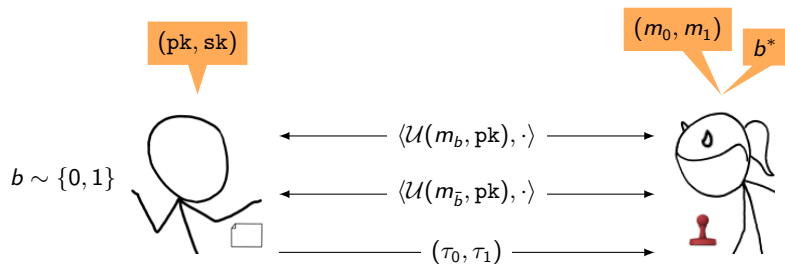
$$(m, \tau)$$



$$\text{Verify}_{\mathcal{R}}((mP + T, P), \sigma, \text{pk}_{\mathcal{R}}) \stackrel{?}{=} 1$$

$$e(R, \hat{Q}) \stackrel{?}{=} e(T, \hat{P})$$

Blindness: Honest-Key Model



Blindness: Honest-Key Model...

Embed DDH instance (P, rP, sP, tP)

$((pk_{\mathcal{R}}, (Q, \hat{Q})), (sk_{\mathcal{R}}, q))$

(m_0, m_1)

b^*

$$b \sim \{0, 1\}$$

$$r_b, s_b \sim \mathbb{Z}_p^*$$

$$r_{\bar{b}}, s_{\bar{b}} \sim \mathbb{Z}_p^*$$



$$\leftarrow \dots (m_b(s_b P) + q(r_b s_b P), P) \dots \rightarrow$$

$$\leftarrow \dots (m_{\bar{b}}(s_{\bar{b}} P) + q(r_{\bar{b}} s_{\bar{b}} P), P) \dots \rightarrow$$

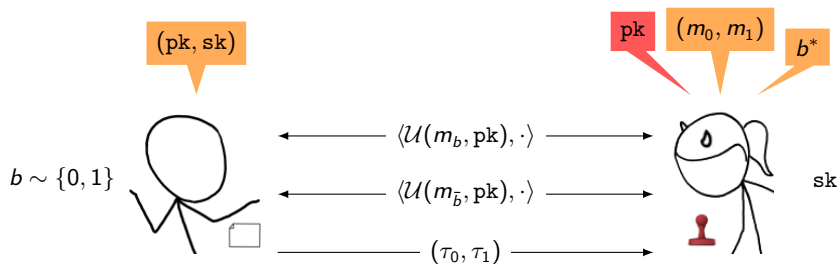
$$\xrightarrow{(\tau_0, \tau_1)}$$



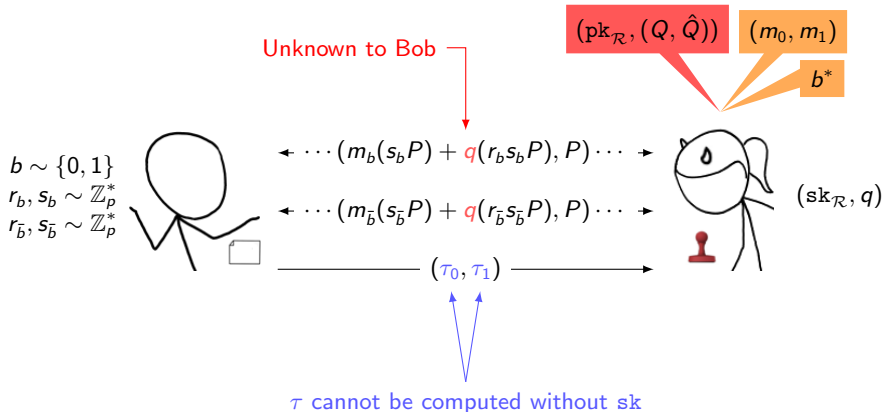
$$\tau = (\sigma, R, T) : \sigma = \text{ChgRep}_{\mathcal{R}}(\cdot, \cdot, 1/s, \cdot)$$

$\text{Sign}_{\mathcal{R}}$ instead of $\text{ChgRep}_{\mathcal{R}}$

Blindness: Malicious-Key Model



Blindness: Malicious-Key Model...



► Solution:

1. **Interactive** variant of DDH needed
2. **Rewind** Alice to generate signatures ($ChgRep_{\mathcal{R}}$ uniform)

Our construction

- ▶ **Idea:** *Bob* chooses parameters for commitment
 - ▶ Must be *perfectly binding*
- ▶ **Bob:**
 1. Chooses “one-time” keys (P, Q) for El-Gamal encryption
 2. Commits to m using $C = mP + rQ$
 3. Obtains signature π from Alice on $\mathbf{M} \sim [(C, rP, Q, P)]_{\mathcal{R}}$
 4. Derives σ on (C, rP, Q, P) using $ChgRep_{\mathcal{R}}$
 5. Outputs $\tau = (\sigma, \text{opening of } C)$ to Charlie

sR allows verification!
 $e(M_1 - mM_4) \stackrel{?}{=} e(M_2, \hat{Q})$

$m \in \mathbb{Z}_p^*$
 $r, s \in \mathbb{Z}_p^*, R = rP$
 $q \in \mathbb{Z}_p^*, Q := qP$



$M = s \cdot (mP + rQ, R, Q, P)$

$pk = pk_{\mathcal{R}}$



$sk = sk_{\mathcal{R}}$

$\pi \leftarrow \text{Sign}_{\mathcal{R}}(M, sk)$

$\sigma \leftarrow \text{ChgRep}_{\mathcal{R}}(M, \pi, 1/s, pk_{\mathcal{R}})$
 $\tau \leftarrow (\sigma, R, Q, Z = rQ, \hat{Q} = q\hat{P})$

Solution: split q

(m, τ)



$\text{Verify}_{\mathcal{R}}((mP + Z, R, Q, P), \sigma, pk_{\mathcal{R}}) \stackrel{?}{=} 1$
 $e(Q, \hat{P}) \stackrel{?}{=} e(P, \hat{Q}), e(Z, \hat{P}) \stackrel{?}{=} e(R, \hat{Q})$

$m \in \mathbb{Z}_p^*$
 $r, s \in \mathbb{Z}_p^*, R = rP$
 $u, v \in \mathbb{Z}_p^*, Q := uvP$



$$M = s \cdot (mP + rQ, R, Q, P)$$

$$\pi \leftarrow \text{Sign}_{\mathcal{R}}(M, \text{sk})$$

pk = pk_ℛ



sk = sk_ℛ

$$\sigma \leftarrow \text{ChgRep}_{\mathcal{R}}(M, \pi, 1/s, \text{pk}_{\mathcal{R}})$$

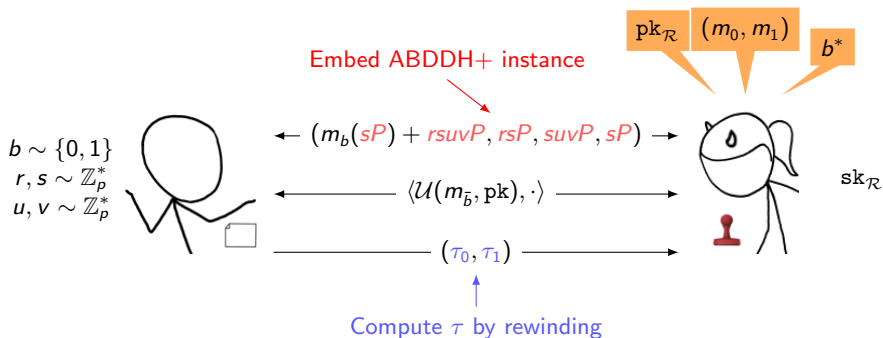
$$\tau \leftarrow (\sigma, R, Q, Y = rQ, U = uP, X = ruP, \hat{U} = u\hat{P}, \hat{V} = v\hat{P})$$

(m, τ)



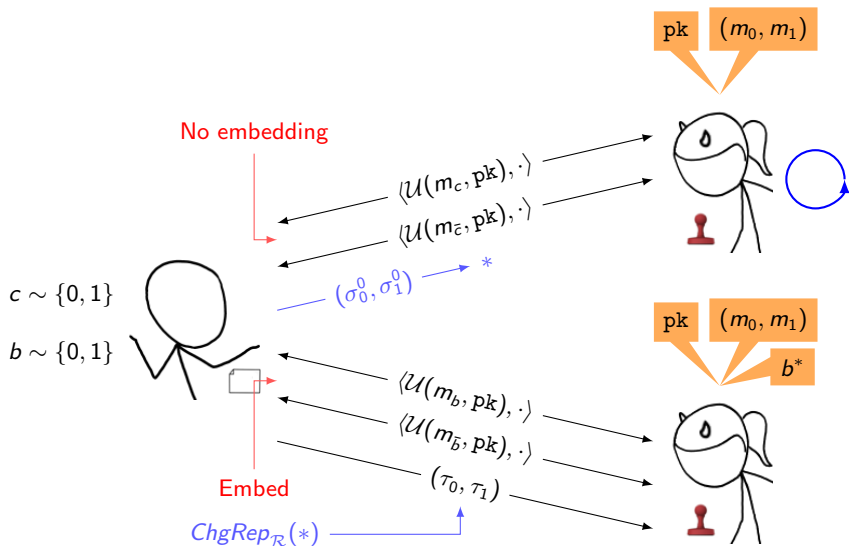
$$\begin{aligned}
 &\text{Verify}_{\mathcal{R}}((mP + Y, R, Q, P), \sigma, \text{pk}_{\mathcal{R}}) \stackrel{?}{=} 1 \\
 &e(Q, \hat{P}) \stackrel{?}{=} e(U, \hat{V}), e(U, \hat{P}) \stackrel{?}{=} e(P, \hat{U}) \\
 &e(X, \hat{P}) \stackrel{?}{=} e(R, \hat{U}), e(Y, \hat{P}) \stackrel{?}{=} e(X, \hat{V})
 \end{aligned}$$

Blindness: Malicious-Key Model



- ▶ ABDDH+ assumption: hard to distinguish $ruvP$ from random given: $rP, uP, uvP, u\hat{P}, v\hat{P}$
 - ▶ $\text{ABDDH+} \implies \text{DDH}$
 - ▶ Hard in generic group model

Blindness: Malicious-Key Model...



- ▶ Multiple rewinds required: fails for single rewind!

Comparison

	[GG14]	[FHS15]	This work
Assumption	DLIN	Interactive DDH	ABDDH+
Public-key	$43G$	$1G_1 + 3G_2$	$4G_2$
Communication	$> 41G$	$4G_1 + 1G_2$	$6G_1 + 1G_2$
Signatures	$183G$	$4G_1 + 1G_2$	$7G_1 + 3G_2$
Computation	$9e$	$7e$	$14e$

References

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